

$$\int (3x^5 - 7x^3 + 8) dx = 3 \frac{x^6}{6} - 7 \frac{x^4}{4} + 8x + C \quad x \in (-\infty, +\infty)$$

$$\int (3\cos x - 7\sin x + 2e^x) dx = 3\sin x + 7\cos x + 2e^x + C$$

$x \in (-\infty, +\infty)$

$$\begin{aligned} \int \frac{(x-2)^2}{x} dx &= \int \frac{x^2 - 4x + 4}{x} dx = \int \left(\frac{x^2}{x} - \frac{4x}{x} + \frac{4}{x} \right) dx = \\ &= \int \left(x - 4 + \frac{4}{x} \right) dx = \frac{x^2}{2} - 4x + 4 \ln|x| + C \end{aligned}$$

$x \in (-\infty, 0) \text{ oder } \in (0, +\infty)$

$$\int \sqrt[4]{x} (4x+12) dx = \int x^{\frac{1}{4}} (4x+12) dx = \int (4x^{\frac{5}{4}} + 12x^{\frac{1}{4}}) dx =$$

$$= 4 \frac{x^{\frac{9}{4}}}{\frac{9}{4}} + 12 \cdot \frac{x^{\frac{5}{4}}}{\frac{5}{4}} + C = \frac{16}{9} \sqrt[4]{x^9} + \frac{48}{5} \sqrt[4]{x^5} + C$$

$x \in (0, +\infty)$

$$\int \frac{x^2 - 2}{x^2 + 1} dx = \int \frac{x^2 + 1 - 3}{x^2 + 1} dx = \int \left(\overset{1}{\frac{x^2 + 1}{x^2 + 1}} - \frac{3}{x^2 + 1} \right) dx =$$

$$= x - 3 \arctan x + C$$

$x \in (-\infty, +\infty)$

Metoda per partes

$$(u \cdot v)' = u' \cdot v + \underline{u \cdot v'}$$

$$\int u \cdot v' = \int (u \cdot v)' - \int u' \cdot v$$

$$\int u \cdot v' = u \cdot v - \int u' \cdot v$$

$$\int x^2 \cos x \, dx = x^2 \sin x - \int 2x \sin x \, dx = x^2 \sin x - (-2x \cos x + 2 \int \cos x \, dx)$$

$$\begin{array}{l} u = x^2 \\ u' = \cos x \end{array} \quad \begin{array}{l} u' = 2x \\ v = \sin x \end{array}$$

$$\begin{array}{l} u = 2x \\ u' = \sin x \end{array} \quad \begin{array}{l} u' = 2 \\ v = -\cos x \end{array}$$

$$= x^2 \sin x + 2x \cos x - 2 \sin x + C$$

$$x \in (-\infty, +\infty)$$

$$\int x^2 \ln x \, dx = \frac{x^3}{3} \ln x - \int \frac{x^3}{3} \cdot \frac{1}{x} \, dx = \frac{x^3}{3} \ln x - \frac{1}{3} \int x^2 \, dx =$$

~~$$u = x^2 \quad u' = 2x$$~~

~~$$v' = \ln x \quad v = ?$$~~

$$= \frac{x^3}{3} \ln x - \frac{x^3}{9} + C$$

$$x \in (0, +\infty)$$

~~$$u = \ln x$$~~

~~$$u' = \frac{1}{x}$$~~

~~$$v' = x^2$$~~

~~$$v = \frac{x^3}{3}$$~~

$$\int x \ln^2 x \, dx = \frac{x^2}{2} \ln^2 x - \int x \cdot \ln x \, dx = *$$

$$u = \ln^2 x \quad u' = 2 \ln x \cdot \frac{1}{x}$$

$$v' = x \quad v = \frac{x^2}{2}$$

$$u = \ln x \quad u' = \frac{1}{x}$$

$$v' = x \quad v = \frac{x^2}{2}$$

$$* = \frac{x^2}{2} \ln^2 x - \left(\frac{x^2}{2} \ln x - \frac{1}{2} \int x \, dx \right) = \frac{x^2}{2} \ln^2 x - \frac{x^2}{2} \ln x + \frac{x^2}{4} + c$$

$$x \in (0, +\infty)$$

$$\ln^2 x = (\ln x)^2 = \ln x - \ln x$$

$$\ln(x^2)$$

$$\int \frac{\ln x}{x} dx = \int \ln x \cdot \frac{1}{x} dx = \ln^2 x - \int \ln x \cdot \frac{1}{x} dx$$

~~$$u = \ln x \quad u' = \frac{1}{x}$$~~

~~$$v' = \frac{1}{x} \quad v = \ln x$$~~

$x \in (0, +\infty)$

$$\int \frac{\ln x}{x} dx = \ln^2 x - \int \frac{\ln x}{x} dx + \int \frac{\ln x}{x} dx$$

$$2 \int \frac{\ln x}{x} dx = \ln^2 x \quad / : 2$$

$$\int \frac{\ln x}{x} dx = \frac{1}{2} \ln^2 x + c$$

$$\int \frac{\ln x}{x} dx = \int t dt =$$

$$\frac{t}{dt} = \frac{\ln x}{\frac{1}{x} dx} = \frac{t^2}{2} + c =$$

$$= \frac{\ln^2 x}{2} + c$$

$$\int \sin^2 x \, dx = -\sin x \cos x + \int \cos^2 x \, dx = -\sin x \cos x + \int (1 - \sin^2 x) \, dx$$

$$~~u = \sin x \quad u' = \cos x~~$$

$$~~v' = \sin x \quad v = -\cos x~~$$

$$\boxed{\sin^2 x + \cos^2 x = 1}$$

$$\cos^2 x = 1 - \sin^2 x$$

$$\int \sin^2 x \, dx = -\sin x \cos x + x - \int \sin^2 x \, dx \quad / + \int \sin^2 x \, dx$$

$$2 \int \sin^2 x \, dx = x - \sin x \cos x \quad / : 2$$

$$\int \sin^2 x \, dx = \frac{x - \sin x \cos x}{2} + c$$

$$\int \sin^2 x \, dx$$

$$\cos 2x = \cos^2 x - \sin^2 x = 1 - 2\sin^2 x \rightarrow \boxed{\sin^2 x = \frac{1 - \cos 2x}{2}}$$

\uparrow
 $\cos^2 x = 1 - \sin^2 x$

$$\int \sin^2 x \, dx = \int \left(\frac{1}{2} - \frac{\cos 2x}{2} \right) dx = \frac{1}{2}x - \frac{\overset{=}{\sin 2x}}{4} + C$$

$\sin 2x = 2\sin x \cos x$