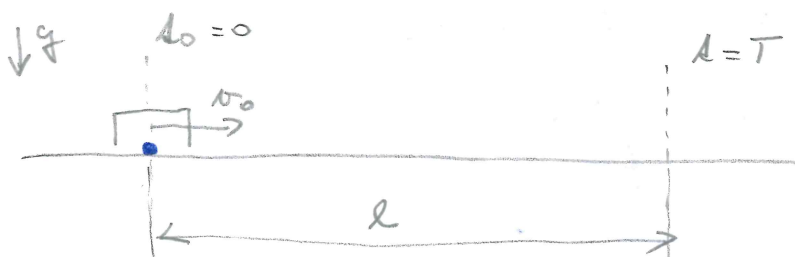


HROTUJÍ BOD SE POHYBUJE PO VODROVNĚ DRSNÉ ROVINĚ
 DRŮŽTE ČAS POTŘEBNÝ K ZASTAVENÍ A BRZDNOU DRŮŽHU

D: m, g, f, v_0

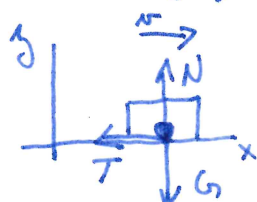
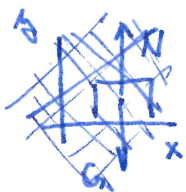
U: a) l ; b) $l = T$



a) KE STANOVENÍ l VTOŽIŠNĚ VZKE

$$K_2 - K_1 = \int_{(M)} \vec{F} \cdot d\vec{x}$$

- KŘIVKOVÝ INTEGRÁL II. DRŮHU



$$\vec{F} = \begin{bmatrix} -T \\ 0 \end{bmatrix} \quad d\vec{x} = \begin{bmatrix} dx \\ 0 \end{bmatrix}$$

$$T = fmg$$

$$K_2 - K_1 = - \int_0^l fmg \, dx$$

$$-\frac{1}{2}mv_0^2 = - [fmgx]_0^l = -(fmg l - 0)$$

$$v_0^2 = 2fgl$$

$$l = \frac{v_0^2}{2fg}$$


b) KE STANOVENÍ DOBY BRZEBŇENÍ VZH

$$\vec{p}_2 - \vec{p}_1 = \int_{t_1}^{t_2} \vec{F} \, dt$$

POHIB PODĚL X: $mv_2 - m_1v_1 = \int_{t_1}^{t_2} F_x \, dt$
 J: $0 = 0$

$$m v(t_2) - m v(t_1) = \int_0^T F_x dt$$
$$- m v_0 = - \int_0^T m g f dt$$

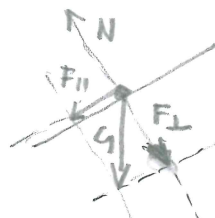
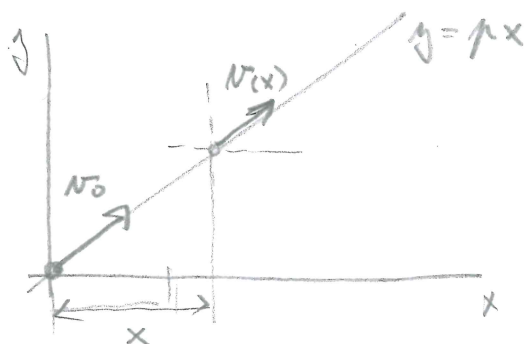
$$m v_0 = m g f [t]_0^T$$

$$T = \frac{v_0}{fg}$$


Hmotný bod se pohybuje po přímce $k: y = \mu x$ v tíhovém poli. Určete rychlost v v závislosti na souřadnici x . Počáteční rychlost je nulová.

D: $v_0; g; k$; nerovnice hmoty

U: $N(x)$



$$K_2 - K_1 = \int_{(m)} \vec{G} \cdot d\vec{r} = \int_{r_1}^{r_2} \vec{G} \cdot d\vec{r}$$

$$K_2 - K_1 = \int_{(P)} (0; -mg) \cdot (dx; dy)$$

$$\begin{aligned} y &= \mu x & (y = y(x)) \\ dy &= \mu dx & \begin{cases} x_0 = 0 \\ x_2 = x \end{cases} \end{aligned}$$

$$K_2 - K_1 = \int_{(P)} (0; -mg) \cdot (dx; \mu dx) \quad x_2 \in \langle 0; x \rangle$$

$$\frac{1}{2} m (v_2^2 - v_1^2) = \int_0^x -mg \mu dx$$

$$v_2^2 - v_0^2 = -2g\mu [x]_0^x$$

$$v_2^2 =$$

$$v^2(x) - v_0^2 = -2g\mu x$$

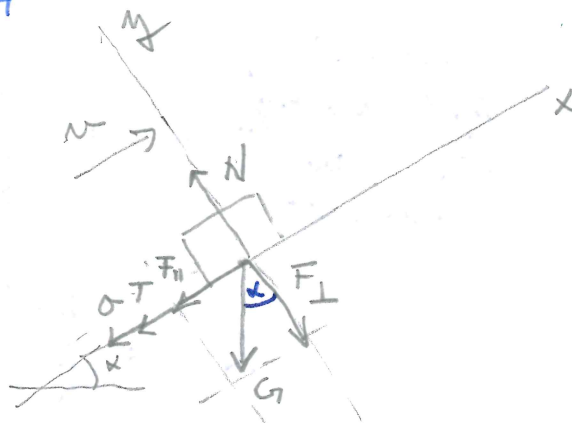
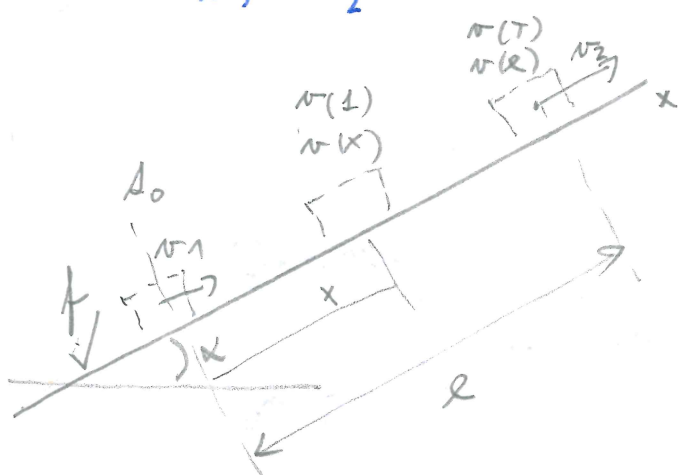
$$v(x) = \pm \sqrt{v_0^2 - 2g\mu x}$$

HMOTNÝ BOD SE POHYBUJE PO DRSNĚ NAKLONĚNÉ ROVINĚ SMĚREM NADOLU. PŘI ZNÁLOSTI POČÁTEČNÍ RYCHLOSTI A SE ZAPŮČETÍM OUPRODU VĚDUCHU $\sigma = c \cdot v$ VŮPOČTĚTE

- a) ZÁVISLOST RYCHLOSTI NA DRÁŽE l
 b) ————— || ————— NA ČASE t

D: m, g, f, μ, v_1 - počáteční; $\sigma = c \cdot v$

- V: a) $v_2(l) = v(x) \rightarrow v \in K E$
 b) $v_2(t) \rightarrow v \in H$



$$F_{||} = -m \cdot g \cdot \sin \alpha$$

$$F_{\perp} = -m \cdot g \cdot \cos \alpha$$

$$T = N \cdot f = m \cdot g \cdot \cos \alpha \cdot f$$

$$F_x = -T - m \cdot g \cdot \sin \alpha - c \cdot v$$

$$F_y = N - m \cdot g \cdot \cos \alpha = 0$$

$$F_x = -N \cdot f - m \cdot g \cdot \sin \alpha - c \cdot v = -m \cdot g (\sin \alpha + f \cdot \cos \alpha) - c \cdot v$$

$$F_x = -c \cdot v - m \cdot g (\underbrace{f \cdot \cos \alpha + \sin \alpha}_{\tilde{g}})$$

$$F_x = -c \cdot v - m \cdot \tilde{g}$$

a) VĚKLE: $K_2 - K_1 = \int_{\vec{r}_1}^{\vec{r}_2} \vec{F} \cdot d\vec{r}$

$$\frac{1}{2} m (v_2^2 - v_1^2) = \int_0^l F_x dx = \int_0^l (-c \cdot v - m \cdot \tilde{g}) dx$$

DIF. TVAR: $dK = \vec{F} \cdot d\vec{r}$

$$m \frac{d\vec{v}}{dt} \cdot d\vec{r} = \vec{F} \cdot d\vec{r}$$

$$K = \frac{1}{2} m v^2$$

$$dK = m \cdot v \cdot dv$$

$$m \vec{v} dv = m \frac{d(v^2)}{2} = \vec{F} \cdot d\vec{r}$$

$$m v dv = (-c v - m \tilde{g}) dx$$

$$\int_{v_1}^{v_2} \frac{m v dv}{-c v - m \tilde{g}} = \int_0^l dx$$

$$\text{FOR: } \begin{aligned} -c v - m \tilde{g} &= u \\ -c dv &= du \\ dv &= -\frac{1}{c} du \end{aligned}$$

$$v_1 \rightsquigarrow -c v_1 - m \tilde{g}$$

$$v_2 \rightsquigarrow -c v_2 - m \tilde{g}$$

$$\frac{m}{c^2} \int_{-c v_1 - m \tilde{g}}^{-c v_2 - m \tilde{g}} \frac{u + m \tilde{g}}{u} du = \int_0^l dx$$

$$l = \frac{m}{c^2} \left[u + m \tilde{g} \ln|u| \right]_{-c v_1 - m \tilde{g}}^{-c v_2 - m \tilde{g}}$$

$$l = \frac{m}{c^2} \left[c v_1 - c v_2 + m \tilde{g} \ln \left(\frac{c v_2 + m \tilde{g}}{c v_1 + m \tilde{g}} \right) \right]$$

$$l = f(v_2)$$

$$v_2 \stackrel{!}{=} f^{-1}(l) \quad - \text{NUMERISCH}$$

b) $v_2(l) = ? \rightarrow VZH$

$$d\vec{p} = \vec{F} dt$$

$$m d\vec{v} = \vec{F} dt$$

$$m dv = (-c v - m \tilde{g}) dt$$

$$\int_{v_1}^{v_2} \frac{m}{-c v - m \tilde{g}} dv = \int_{t_1}^{t_2} dt$$

$$T = \int_{v_1}^{v_2} \frac{m}{-c v - m \tilde{g}} dv \stackrel{\text{SUB.}}{=} -\frac{1}{c} \int_{-c v_1 - m \tilde{g}}^{-c v_2 - m \tilde{g}} \frac{du}{u} = -\frac{1}{c} \ln \frac{c v_2 + m \tilde{g}}{c v_1 + m \tilde{g}}$$

$$v_2 = \left[e^{-T c} \cdot (c v_1 + m \tilde{g}) - m \tilde{g} \right] \frac{1}{c}$$